# A calculation method for low dynamic vehicle velocity based on fusion of optical flow and feature point matching

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Abstract: Aiming at the problem of the low accuracy of low dynamic vehicle velocity under the environment of uneven distribution of light intensity, an improved adaptive Kalman filter method for the velocity error estimate by the fusion of optical flow tracking and scale invariant feature transform (SIFT) is proposed. The algorithm introduces a nonlinear fuzzy membership function and the filter residual for the noise covariance matrix in the adaptive adjustment process. In the process of calculating the velocity of the vehicle, the tracking and matching of the inter-frame displacement and the vehicle velocity calculation are carried out by using the optical flow tracing and the SIFT methods, respectively. Meanwhile, the velocity difference between the outputs of these two methods is used as the observation of the improved adaptive Kalman filter. Finally, the velocity calculated by the optical flow method is corrected by using the velocity error estimate of the output of the modified adaptive Kalman filter. The results of semi-physical experiments show that the maximum velocity error of the fusion algorithm is decreased by 29% than that of the optical flow method, and the computation time is reduced by 80% compared with the SIFT method.

**Key words:** velocity; optical flow; feature point matching; non-uniform light intensity distribution

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T raditionally, the task of computing speed is usually performed using imprecise wheel speed sensors and inertial measurement units<sup>[1]</sup> or expensive high accuracy inertial measurement units<sup>[2]</sup>. In recent years, it has become an important requirement to obtain the speed of the vehicle based on vision. In comparison with wheel odometry, the visual method is not affected by wheel slippage in slippery or uneven terrain or other abnormal conditions, which can provide more accurate speed estimates<sup>[3]</sup>. The visual method is useful for various reasons due to the fact that cameras are fairly small and inexpensive, and they can obtain a greater data stream of the surrounding environment, by which the speed of the robot or vehicle can be accurately estimated<sup>[4]</sup>.

In a uniform light intensity distribution environment, the visual method of obtaining velocity has high precision and is an excellent complement to wheel odometry or other navigation systems such as the global positioning system or inertial measurement units<sup>[5]</sup>. In Ref. [6], the BRISK and SURF feature point matching algorithms are used to measure the vehicle speed, which can ensure the robustness in the uneven distribution of light intensity, but the real-time performance is poor. Kitt et al.<sup>[7]</sup> proposed a robust optical flow method for accurately estimating the attitude of UAV, which is fast and the image motion estimation meets the requirements of high precision and stability, nevertheless the accuracy of the motion velocity estimated by this method is markedly influenced by illumination.

In this paper, a new method is proposed to calculate the velocity of a low dynamic vehicle, which is based on the fusion of optical flow and feature matching under the condition of uneven distribution of light intensity. By the vehicle driving test in a non-uniform intensity environment, the results show that this method overcomes the shortcomings of the optical flow and the SIFT feature matching methods while the estimation accuracy and realtime performance are improved significantly.

### 1 Fusion Model

# **1.1** Image velocity estimation based on optical flow computation

The Lucas-Kanade optical flow algorithm proposed by Lucas et al.<sup>[8]</sup> has been widely used for optical flow estimation, which is used to obtain the optical flow value by assuming that the optical flow in the local neighborhood of the pixel of interest is invariant and then solving the elementary optical flow equation constructed by all the pixels around the neighborhood of the pixel of interest by the least square method. Bouguet<sup>[9]</sup> proposed a Lucas-Kanade algorithm based on pyramid layering to cope with the problem of using the Lucas-Kanade algorithm, which means that the condition that the inter-frame displacement

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should be small enough must be satisfied. This algorithm is summarized in the following.

For a point  $u(u_x, u_y)$  in the current frame image  $I_{k-1}$ , a point  $v(u_x + d_x, u_y + d_y)$  is found in the next frame image  $I_k$ , which has the most similar gray values to  $u(u_x, u_y)$  and the vector  $\boldsymbol{d} = [d_x, d_y]$  represents the optical flow of the pixel u.

We define the gray value difference between the two consecutive frames as

$$\varepsilon(\boldsymbol{d}, \boldsymbol{A}) = \varepsilon(d_{x}, d_{y}, d_{xx}, d_{xy}, d_{yx}, d_{yy}) = \sum_{x = -w_{x}}^{w_{x}} \sum_{y = -w_{y}}^{w_{y}} (I_{k-1}(x + u_{x}, y + u_{y}) - I_{k}([x, y]\boldsymbol{A}^{\mathrm{T}} + \boldsymbol{d} + u))$$
(1)

where  $A = \begin{bmatrix} 1 + d_x & d_{xy} \\ d_{yx} & 1 + d_{yy} \end{bmatrix}$  is the transformation matrix, and  $d_{xy}$ ,  $d_{yy}$ ,  $d_{yx}$  and  $d_{yy}$  are the affine deformation param-

and  $a_{xx}$ ,  $a_{xy}$ ,  $a_{yx}$  and  $a_{yy}$  are the armie deformation parameters.

This algorithm achieves the purpose of calculating the optical flow by finding vector d and transformation matrix A, so that the gray scale difference of the consecutive frames is minimum.

This algorithm also needs to build an image pyramid by down-sampling. First, the optical flow is calculated by the top-level image in the image pyramid, and then the optical flow is used to estimate the position of the corresponding pixel in the next layer pyramid. These processes are repeated until the image pyramid of the bottom is calculated. According to this method, the horizontal and vertical displacements of the feature points of the consecutive frames are tracked and matched. Subsequently, all the displacement is accumulated and averaged to obtain the pixel displacement [ $s_{Lx}$   $s_{Ly}$ ]<sup>T</sup> between the consecutive frames. The image pixel velocity [ $v_{Lx}$   $v_{Ly}$ ]<sup>T</sup> can be calculated as

$$\begin{bmatrix} v_{Lx} & v_{Ly} \end{bmatrix}^{\mathrm{T}} = f \begin{bmatrix} s_{Lx} \\ s_{Ly} \end{bmatrix}$$
(2)

where f is the frequency of the camera.

## 1.2 Image velocity estimation based on SIFT matching

In this paper, SIFT<sup>[10]</sup> is used to extract feature points for matching, so as to estimate the speed between two adjacent frames. First, the SIFT feature matching algorithm is used to establish the scale space, and the representation of an image in different scale space can be obtained by convolving the original image I with a set of variablescaled Gaussian G:

$$L(x, y, \sigma) = G(x, y, \sigma) * I(x, y)$$
(3)

where *L* stands for the scale space and  $\sigma$  denotes the scale space factor.

In order to ensure that the extreme stable points are de-

tected in both the scale space and two-dimensional image space, the DOG (difference-of-Gaussian) operator is applied to approximate the Laplacian-Gaussian operator. Suppose that the approximate operator is  $D(x, y, \sigma)$ , after processing the image, we have

$$D(x, y, \sigma) = L(x, y, k\sigma) - L(x, y, \sigma)$$
(4)

where k is the constant factor.

After approximating the Laplacian-Gaussian operator by the DOG operator, extrema detection is required in DOG scale space. The gray scale value of the point to be detected is compared with 18 pixels at the corresponding position of the front and rear images in the scale space, as well as the surrounding ones of the point itself. Altogether, a single point requires 26 comparisons. When an extremum (maximum or minimum) is detected, it is kept for further processing.

Local extrema detected in DOG scale-space are called keypoints after the operations of improving positioning accuracy and eliminating low-contrast points. To locate the keypoints accurately, the principal curvature and keypoint orientation should be determined. The principal curvature calculated by the Hessian matrix and a threshold is used to remove the unstable edge response. The orientation is determined by the distribution characteristics of the gradient magnitude of the keypoints. The gradient magnitude m(x, y) and orientation  $\theta(x, y)$  can be expressed as

$$m(x, y) = ((L(x+1, y) - L(x-1, y))^{2} + (L(x, y+1) - L(x, y-1))^{2})^{1/2}$$
(5)

$$\theta(x, y) = \tan^{-1} \left( \frac{L(x, y+1) - L(x, y-1)}{L(x+1, y) - L(x-1, y)} \right)$$
(6)

An orientation histogram is formed from the gradient orientations  $\theta$  of sample points in the region around the keypoints, and the peak of the histogram as the main direction of the keypoint while the information of the key point is given and it is further descripted by generating the eigenvector descriptor.

After the descriptor is generated, the Euclidean distance of the feature vector is used as the feature point matching criterion, and the image velocity is calculated by the successful matched feature points.

$$\begin{bmatrix} v_{Sx} \\ v_{Sy} \end{bmatrix} = f \begin{bmatrix} s_{Sx} \\ s_{Sy} \end{bmatrix}$$
(7)

where  $s_{sx}$  is the average horizontal displacement of feature points, and  $s_{sy}$  is the vertical displacement.

# **1.3** The relationship between vehicle velocity and image velocity

In our experiments, the camera is mounted on the front of the vehicle and the optical axis is perpendicular to the ground surface to achieve the vertical photography of the ground texture<sup>[11-12]</sup>. The speed measurement model is shown in Fig. 1.  $P(X_R, Y_R, Z_R)$  is a point on the ground which is projected onto the normalized image plane.  $Z_R$  is the distance from the camera projection center to the ground, and *R* is the projection point of the optical center of the camera on the ground.



Fig. 1 Speed measurement model

The relationship between the projection point  $P'(x_n, y_n, z_n)$  and  $P(x_n, y_n, z_n)$  can be expressed as

$$\begin{bmatrix} x_n \\ y_n \\ 1 \end{bmatrix} = \begin{bmatrix} X_R/Z_R \\ Y_R/Z_R \\ 1 \end{bmatrix}$$
(8)

Taking the camera lens distortion effects into account,  $P'(x_n, y_n, z_n)$  is the actual image point and  $P''(x_d, y_d, z_d)$  is the ideal image point. The relationship of the distortion correction is

$$\begin{bmatrix} x_d \\ y_d \end{bmatrix} = (1 + k_1 r^2) \begin{bmatrix} x_n \\ y_n \end{bmatrix} + \begin{bmatrix} 2p_1 x_n y_n + p_2 (r^2 + 2x_n^2) \\ p_1 (r^2 + 2y_n) + 2p_2 x_n y_n \end{bmatrix} (9)$$

where  $r = \sqrt{x_n^2 + y_n^2}$ ;  $k_1$  is the coefficient of radial distortion;  $p_1$  and  $p_2$  denote the coefficients of axial distortion.

In order to estimate the velocity of the vehicle,  $P''(x_d, y_d, z_d)$  is mapped to the point  $P'''(x_p, y_p, z_p)$  in the physical image coordinate system. The specific mapping relationship is

$$\begin{bmatrix} x_p \\ y_p \end{bmatrix} = \begin{bmatrix} \alpha_x & \alpha_x \gamma \\ 0 & \alpha_y \end{bmatrix} \begin{bmatrix} x_d \\ y_d \end{bmatrix} + \begin{bmatrix} u_0 \\ v_0 \end{bmatrix}$$
(10)

where  $\alpha_x$  and  $\alpha_y$  are the focal distances expressed in units of horizontal and vertical pixels;  $\gamma$  is the skewness coefficient; and  $(u_0, v_0)$  denotes the principal point coordinate of the image plane.

In order to simplify the calculation, we assume that there is no distortion effect in the camera lens, so  $k_1$ ,  $p_1$ ,  $p_2$  and  $\gamma$  are 0. Eq. (10) can be rewritten as

$$\begin{bmatrix} X_R \\ Y_R \end{bmatrix} = \begin{bmatrix} \frac{(x_p - u_0)Z_R}{\alpha_x} \\ \frac{(y_p - v_0)Z_R}{\alpha_y} \end{bmatrix}$$
(11)

Differentiating time in Eq. (11), the velocity of the vehicle can be derived from the *x* and *y* axes of the world coordinate system:

$$\begin{bmatrix} V_x \\ V_y \end{bmatrix} = \begin{bmatrix} \frac{Z_R v_x}{\alpha_x} + \frac{(x_p - u_0) V_Z}{\alpha_x} \\ \frac{Z_R v_y}{\alpha_y} + \frac{(y_p - u_0) V_Z}{\alpha_y} \end{bmatrix}$$
(12)

where  $v_x$  and  $v_y$  represent the pixel speed of the images. It is assumed that the terrain surface is flat during the movement of the vehicle, so  $V_z = 0$  and Eq. (12) can be simplified as

$$\begin{bmatrix} V_x \\ V_y \end{bmatrix} = \begin{bmatrix} \frac{Z_R v_x}{\alpha_x} \\ \frac{Z_R v_y}{\alpha_y} \end{bmatrix}$$
(13)

The vehicle velocity  $\begin{bmatrix} V_{Lx} & V_{Ly} \end{bmatrix}^{T}$  solved by the optical flow method can be obtained from Eqs. (2) and (13), and the velocity  $\begin{bmatrix} V_{Sx} & V_{Sy} \end{bmatrix}^{T}$  solved by feature matching can be obtained by Eqs. (7) and (13).

#### 1.4 Fusion of optical flow and feature point matching

In this paper, an improved adaptive Kalman filter is proposed to fuse the optical flow and the feature matching to calculate the velocity of the vehicle so as to overcome the problems of the low precision of the pyramid Lucas-Kanade optical flow and time-consuming of the SIFT feature matching. Fig. 2 illustrates the fusion algorithm using a block diagram.



Fig. 2 The structure diagram of the fusion algorithm

In the case when the vehicle only moves forward, the velocity in the traveling direction of the vehicle can be expressed by  $V_{Ly}$  and  $V_{Sy}$ . The acceleration difference  $V_a$  and the speed difference  $\Delta V^*$  are the state variables which are solved by the improved adaptive Kalman filter. The difference  $\Delta V$  between  $V_{Ly}$  and  $V_{Sy}$  obtained by visual measurement at each moment is regarded as a measurement.

In general, the calculation speed of the optical flow is faster than that of the SIFT in calculating the visual velocity information. In order to realize the synchronization of speed, the displacement between two consecutive frames is calculated and accumulated by the optical flow method. The average vehicle speed is obtained every 10 frames, and the first and tenth frames are matched by using SIFT to obtain another vehicle speed. Finally, the fusion of these two speeds is carried out.

The state model and measurement model of the filter are shown as follows:

$$\boldsymbol{X}(k) = \boldsymbol{\Phi}(k \mid k-1)\boldsymbol{X}(k-1) + \boldsymbol{U}(k-1)\Delta \overline{a} + \boldsymbol{W}(k-1)$$
(14)

$$\mathbf{Z}(k) = \mathbf{H}(k)\mathbf{X}(k) + \mathbf{V}(k)$$
(15)

where  $\boldsymbol{\Phi}(k \mid k-1) = \begin{bmatrix} 1 & \frac{1-e^{-aT}}{\alpha} \\ 0 & e^{-aT} \end{bmatrix}$ ; *T* is the sampling

period;  $\alpha$  is the reciprocal of the time constant of the acceleration difference;  $\Delta \overline{a}$  is taken as the estimated value of the acceleration difference  $\Delta a(k \mid k - 1)$  at time k;  $U(k-1) = \begin{bmatrix} T - \frac{1 - e^{-\alpha T}}{\alpha} & 1 - e^{-\alpha T} \end{bmatrix}^{T}$ ;  $H(k) = \begin{bmatrix} 1 & 0 \end{bmatrix}$ ;

V(k) stands for the noise of the measurement model.

The covariance matrix Q(k-1) of the system noise is

$$Q(k-1) = 2\alpha\sigma^{2} \begin{bmatrix} \frac{4e^{-\alpha T} - 3 - e^{-2\alpha T} + 2\alpha T}{2\alpha^{3}} & \frac{e^{-2\alpha T} + 1 - 2e^{-\alpha T}}{2\alpha^{2}} \\ \frac{e^{-2\alpha T} + 1 - 2e^{-\alpha T}}{2\alpha^{2}} & \frac{1 - e^{-2\alpha T}}{2\alpha} \end{bmatrix}$$
(16)

The adaptive implementation of the algorithm is based on the current acceleration difference  $\Delta a(k \mid k)$  and the filter residual error err(k) of the vehicle, which adjust the variance  $\sigma^2$  of the current acceleration difference, to fulfill the adaptive adjustment of Q(k-1). The variance  $\sigma^2$ of the acceleration difference is given by

$$\sigma^{2} = \begin{cases} \frac{4 - \pi}{\pi} [\Delta a_{\text{new-max}} - \Delta a(k \mid k)]^{2} & \Delta a(k \mid k) \ge 0\\ \frac{4 - \pi}{\pi} [\Delta a_{\text{new-min}} - \Delta a(k \mid k)]^{2} & \Delta a(k \mid k) < 0 \end{cases}$$
(17)

where  $\Delta a_{\text{new-max}}$  and  $\Delta a_{\text{new-min}}$  are the maximum and the minimum value, which can be achieved after the adaptive adjustment of the acceleration difference. And, they change with the change of  $\Delta a(k \mid k)$ .

 $\Delta a_{-up}$  and  $\Delta a_{up}$  are the limit values of the acceleration difference of the vehicle before adjustment, so the acceleration difference of the vehicle is within the interval  $[\Delta a_{-up}, \Delta a_{up}]$  and the two thresholds  $\Delta a_y$  and  $\Delta a_{-y}$  are set such that  $\Delta a_y > \Delta a_{up}$  and  $\Delta a_{-y} < \Delta a_{-up}$ , then the value of  $\Delta a_{new-max}$  and  $\Delta a_{new-min}$  are adjusted by the nonlinear fuzzy membership function of the exponential form.  $\Delta a_{new-max}$  and  $\Delta a_{new-min}$  are obtained by

$$M = \begin{cases} 1 - k_1^{\Delta a(k|k)} & \Delta a_{up} \ge \Delta a(k \mid k) \ge 0\\ 1 - k_2^{-\Delta a(k|k)} & 0 > \Delta a(k \mid k) \ge \Delta a_{-up} \end{cases}$$
(18)

$$\Delta a_{\text{new-max}} = M\Delta a_{y} \qquad \Delta a(k \mid k) \ge 0$$
  
$$\Delta a_{\text{new-min}} = M\Delta a_{-y} \qquad \Delta a(k \mid k) < 0$$
(19)

In order to further improve the estimation accuracy of the filtering algorithm, the filter residual error err(k) is introduced to adjust coefficients  $k_1$  and  $k_2$ .  $k_1$  and  $k_2$  can be expressed as

$$k_{1} = \begin{cases} (1 - k_{11}^{\parallel \operatorname{err}(k) \parallel_{F}}) \left(\frac{\Delta a_{y} - \Delta a_{up}}{\Delta a_{y}}\right)^{1 \Delta a_{\varphi}} & \parallel \operatorname{err}(k) \parallel_{F} \ge n \\ k_{12} & \parallel \operatorname{err}(k) \parallel_{F} < n \end{cases}$$
(20)

$$k_{2} = \begin{cases} (1 - k_{21}^{\|\operatorname{err}(k)\|_{F}}) \left(\frac{-\Delta a_{-y} - \Delta a_{up}}{-\Delta a_{-y}}\right)^{1/\Delta a_{up}} & \|\operatorname{err}(k)\|_{F} \ge n \\ k_{22} & \|\operatorname{err}(k)\|_{F} < n \end{cases}$$
(21)

$$\operatorname{err}(k) = \mathbf{Z}(k) - \mathbf{H}(k)\mathbf{X}(k \mid k-1)$$
(22)

where *n* is a positive number set according to human experience and only when  $\|\operatorname{err}(k)\|_{\mathrm{F}} \ge n$ ;  $k_1$  and  $k_2$  are adjusted adaptively;  $k_{11}$ ,  $k_{12}$ ,  $k_{21}$  and  $k_{22}$  are constants. The value of  $k_{11}$  is in the interval  $\left[0, \left(1 - \exp\left(\frac{4}{\Delta a_y(\pi - 4)}\right) \left(\frac{\Delta a_y - \Delta a_{\mathrm{up}}}{\Delta a_y}\right)^{-1/\Delta a_{\mathrm{w}}}\right)^{1/n}\right]$ ; the value space of  $k_{12}$  is  $\left[\exp\left(\frac{4}{\Delta a_y(\pi - 4)}\right), \left(\frac{\Delta a_y - \Delta a_{\mathrm{up}}}{\Delta a_y}\right)^{1/\Delta a_{\mathrm{w}}}\right]$ ; the value of  $k_{21}$  is in the interval  $\left[0, \left(1 - \exp\left(\frac{4}{-\Delta a_{-y}(\pi - 4)}\right) \left(\frac{-\Delta a_{-y} - \Delta a_{\mathrm{up}}}{-\Delta a_{-y}}\right)^{-1/\Delta a_{\mathrm{w}}}\right)^{1/n}\right]$ ; and the range of  $k_{22}$  is  $\left[\exp\left(\frac{4}{-\Delta a_{-y}(\pi - 4)}\right), \left(\frac{-\Delta a_{-y} - \Delta a_{\mathrm{up}}}{-\Delta a_{-y}}\right)^{1/\Delta a_{\mathrm{w}}}\right]$ . Finally, the modified adaptive Kalman filter is used to

Finally, the modified adaptive Kalman filter is used to directly correct the vehicle velocity solved by the optical flow, which can achieve higher precision vehicle speed.

#### 2 Simulation Results

Our velocity measurement system consists of a vehicle, a downward-looking camera, a PC, a DC motor and its built-in encoder (see Fig. 3). In the experiment, we con-



Fig. 3 Velocity measurement system

trol the vehicle running in the indoor light intensity distribution uneven environment with a downward-looking camera mounted on the front of the vehicle to acquire image sequences of a carpeted floor surface at a frame rate of 20 frame/s, and each frame image has a  $320 \times 240$  pixels resolution. An encoder is provided on the wheel of the vehicle to collect the vehicle velocity  $V_{\rm E}$ , and the velocity information as a reference value is used to compare the corrected velocity. The speed of the vehicle is about 15 cm/s.

We can see from Fig. 4 that the speed of the SIFT measurement is less affected by the intensity of light than that measured by the optical flow. In Fig. 5,  $T_{\rm F}$  and  $T_{\rm S}$  represent the time consumed by the optical flow and the SIFT, which illustrates that the real-time performance of the optical flow is better than that of the SIFT. As shown in Fig. 6, after using the fusion algorithm of optical flow



Fig. 4 Comparison of the velocity measured by optical flow, SIFT and encoder



**Fig.6** Velocity measured by the encoder and the optical flow before and after the correction

and feature matching, the corrected vehicle velocity  $V_{\rm CL}$  is less affected by the light intensity and it tends to the true value of the speed of the vehicle. Fig. 7 presents that the error curve  $e_{\rm CL}$  of the corrected speed has a smaller fluctuation than that previous correction and  $e_{\rm CL}$  tends to zero. In brief, we can obtain a higher accuracy of the vehicle speed based on the combination of optical flow and feature point matching.



Fig.7 Velocity error before and after correction

### 3 Conclusion

In this paper, we present an improved adaptive Kalman filter to fuse the optical flow tracking method with the SIFT feature matching to solve the problem of the low accuracy of the low dynamic vehicle velocity calculation under the non-uniform light intensity distribution. The experimental results show that the fusion algorithm not only highlights the real-time characteristics of optical flow and the accuracy of SIFT feature matching, but also improves the estimation accuracy and real-time performance of low dynamic vehicle velocity under non-uniform light intensity distribution. The algorithm is instructive to visually aid navigation.

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## 基于光流和特征点匹配相融合的低动态载体速度计算方法

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摘要:针对光强分布不均匀环境下低动态载体速度计算精度低的问题,提出了一种改进自适应卡尔曼滤波方法 应用于光流跟踪与尺度不变特征变换(SIFT)相融合的速度误差估计.该算法引入了一种非线性模糊隶属度函 数和滤波残差用于自适应调整过程噪声的协方差矩阵.在计算载体速度过程中,首先利用光流跟踪法和 SIFT 方法分别进行帧间位移的跟踪和匹配并计算出载体的速度,同时将这2种方法求取的速度做差作为改进的自 适应卡尔曼滤波器的观测量,最后使用改进的自适应卡尔曼滤波器输出的速度误差估计值对光流法求取的速 度进行校正.半物理实验结果表明,该算法求解的最大速度误差较光流法减小了 29%,且运算时间较 SIFT 方 法减少约 80%.

关键词:速度;光流法;特征点匹配;光强分布不均匀 中图分类号:TP242.6